



Adsorption and reaction of hydrogen atoms on graphitic surfaces

Rocco Martinazzo

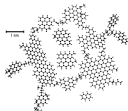
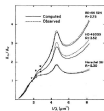
Dipartimento di Chimica
Università degli Studi, Milano, Italy

*Exploring mechanisms for H_2 formation on very small
carbonaceous grains and PAHs of astrophysical interest*
Toulouse, April 25, 2013



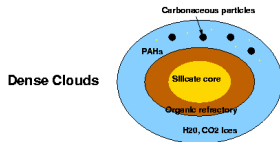
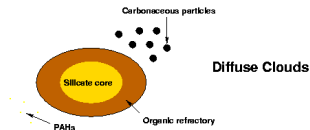
H₂ in the ISM

- Hydrogen is the most abundant element of the Universe
- H₂ is formed on the surface of *dust* grain

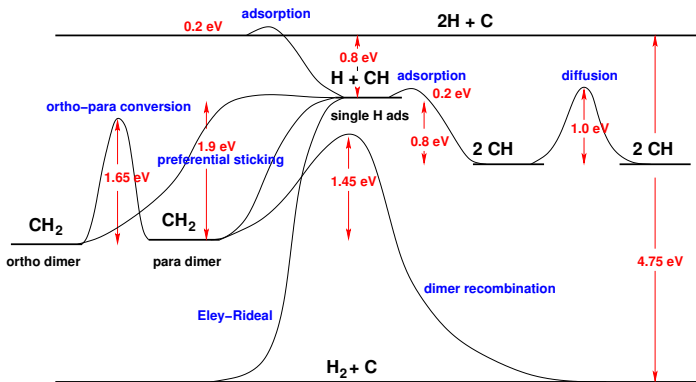


Hydrogen-graphite is an important model for understanding H₂ formation in ISM

$$f_{\text{grain}} = n_{\text{grain}}/n_{\text{H}} \sim 10^{-12} \text{ i.e. } \sim 1\% \text{ of ISM mass}$$



Chemisorption and reaction



R. Martinazzo, S. Casolo and L. Horneaker
in *Dynamics of Gas-Surface Interactions*, Ed.s R. D. Muino and H. F. Busnengo, Springer (2013)

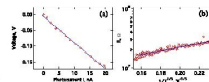
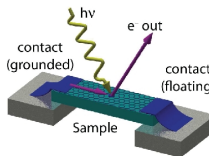
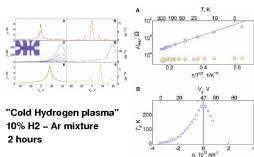




Technology: graphene physics and devices

Graphene is a true **2D-electron gas** (2DEG) system with pseudo-relativistic charge-carriers

MIT occurs when **hydrogenating** graphene



UHV ($p \sim 10^{-9}$ torr)
 $T(\text{H}_2) \sim 2000 \text{ C}$

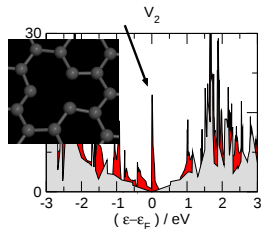
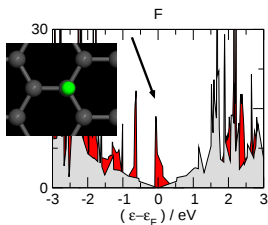
.. σ vs T agrees well with VRH in two dimensions

High n_H : D. C. Elias *et al.*, *Science* **323**, 610 (2009)

Low n_H : A. Bostwick *et al.*, *Phys. Rev. Lett.* **103**, 056404 (2009)



p_z vacancies



- Midgap states show up in the DOSs
- H, F, OH, CH₃, etc. behave similarly to vacancies





Outline

1 Point defects in graphene

- H adsorption and clustering
- Edge effects
- Vacancies

2 Eley-Rideal reaction

- Quantum Dynamics at high E_{coll}
- Quantum Dynamics at cold E_{coll}
- Ab initio molecular dynamics





Outline

- 1 Point defects in graphene
 - H adsorption and clustering
 - Edge effects
 - Vacancies

- 2 Eley-Rideal reaction
 - Quantum Dynamics at high E_{coll}
 - Quantum Dynamics at cold E_{coll}
 - Ab initio molecular dynamics





Outline

1 Point defects in graphene

- H adsorption and clustering
- Edge effects
- Vacancies

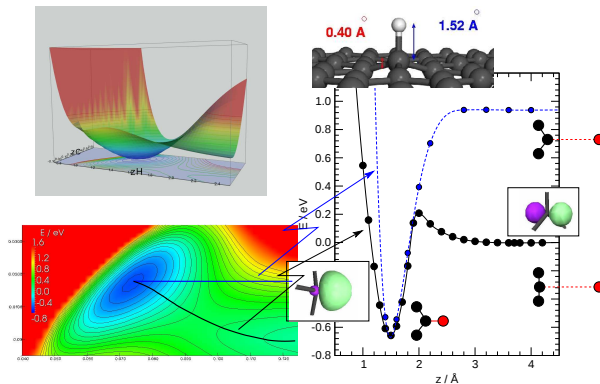
2 Eley-Rideal reaction

- Quantum Dynamics at high E_{coll}
- Quantum Dynamics at cold E_{coll}
- Ab initio molecular dynamics





Single-H chemisorption

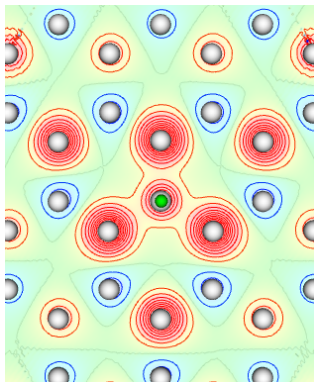


L. Jelaica and V. Sidis, *Chem. Phys. Lett.* **300**, 157 (1999)

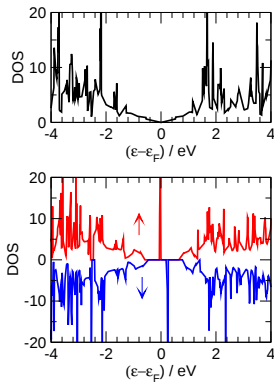
X. Sha and B. Jackson, *Surf. Sci.* **496**, 318 (2002)



Midgap states



..patterned spin-density



Graphene

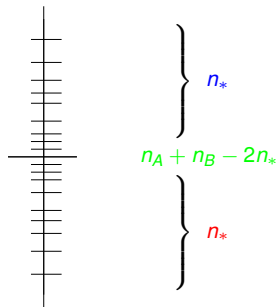
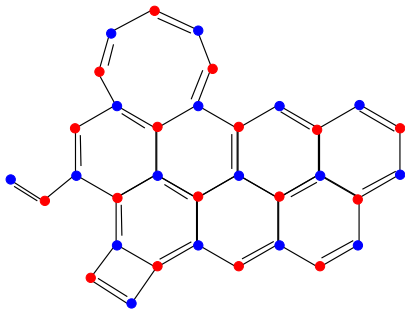
+ H

H-Graphene



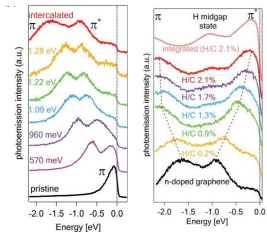
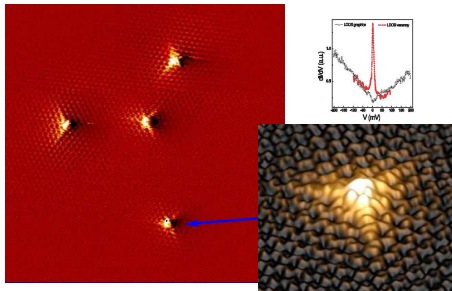
Midgap states

$$H^\pi \approx \sum_{\tau, ij} (t_{ij} a_{i,\tau}^\dagger b_{j,\tau} + t_{ji} b_{j,\tau}^\dagger a_{i,\tau}) + U \sum_i n_{i,\tau} n_{i,-\tau}$$





Midgap states

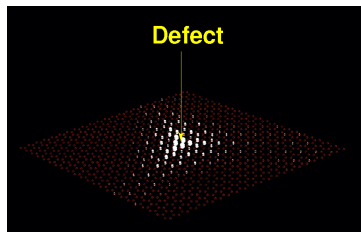


M.M. Ugeda, I. Brihuega, F. Guinea and J.M. Gomez-Rodriguez, *Phys. Rev. Lett.* **104**, 096804 (2010)
 D. Haberer *et al.*, *Phys. Rev. B* **83**, 165433 (2011)



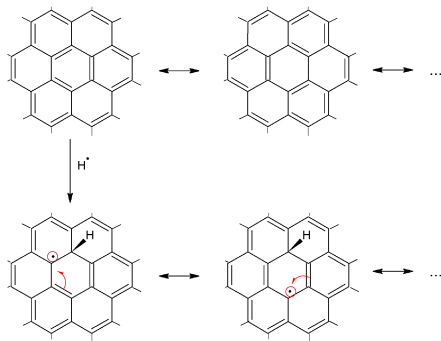


Midgap states



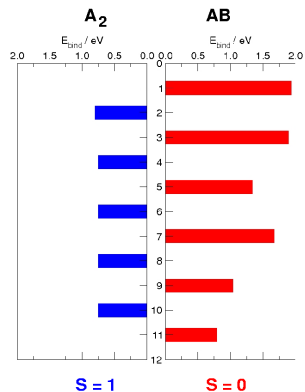
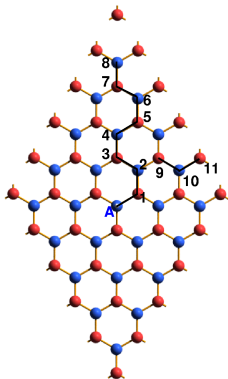
$$\psi(x, y, z) \sim 1/r$$

V. M. Pereira *et al.*, *Phys. Rev. Lett.* **96**, 036801 (2006);
Phys. Rev. B **77**, 115109 (2008)



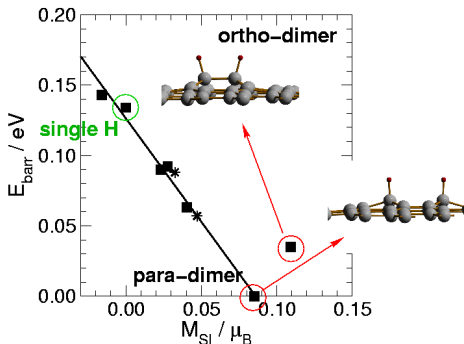
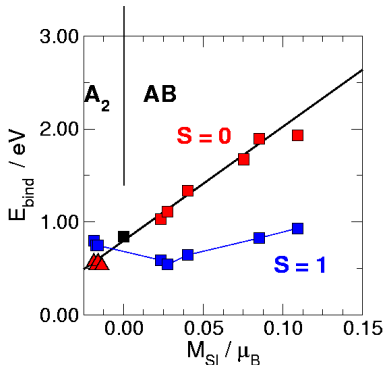


Dimers





Dimers



S. Casolo, O.M. Lovvik, R. Martinazzo and G.F. Tantardini, *J. Chem. Phys.* **130** 054704 (2009)

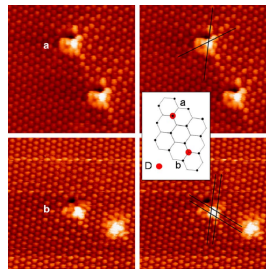
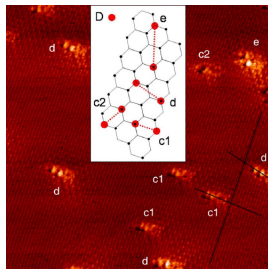
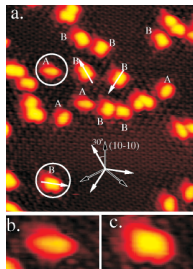
arXiv:0808.1312 (2008)

Preferential sticking: L. Hornekaer *et al.*, *Phys. Rev. Lett.* **96** 156104 (2006)





Dimers

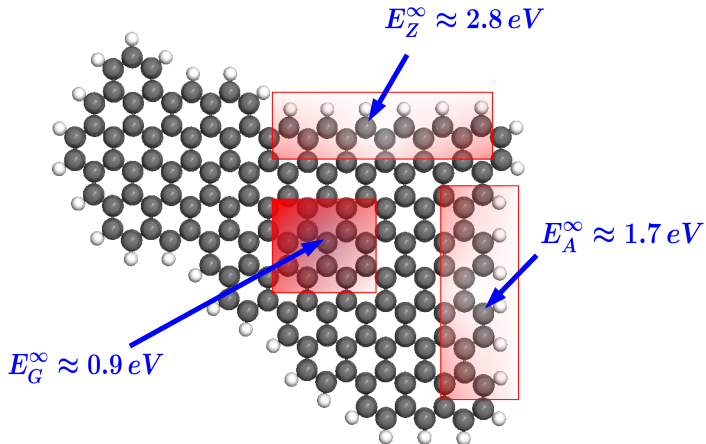


[1] L. Hornekaer, Z. Slijvančanin, W. Xu, R. Otero, E. Rauls, I. Stensgaard, E. Laegsgaard, B. Hammer and F. Besenbacher. *Phys. Rev. Lett.* **96** 156104 (2006)

[2] A. Andree, M. Le Lay, T. Zecho and J. Kupper, *Chem. Phys. Lett.* **425** 99 (2006)



Role of edges





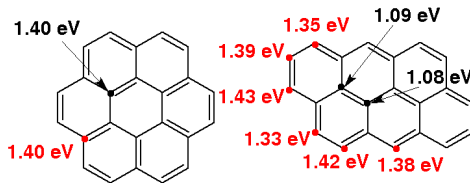
'Geometric' effect?

'Reorganization' energy
upon binding

$$\delta E = E(\text{PAH}^*) - E(\text{PAH}^{\text{eq}})$$

E sites: $\delta E \sim 1.4 \pm 0.1 \text{ eV}$

G sites: $\delta E \sim 1.0 \pm 0.1 \text{ eV}$



...purely **electronic** effect





Hints from the tight-binding Hamiltonian H_π

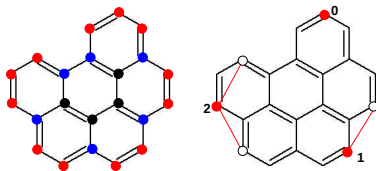
Shape of low-energy orbitals

..from a 'lattice renormalization'

- Coordination (Z)
- Hypercoordination (ξ)
- sublattice imbalance (η)

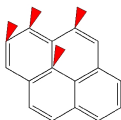
$$Z = 2 \Rightarrow \text{E}$$

$$Z = 3 \Rightarrow \text{F, G}$$

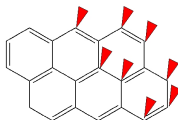




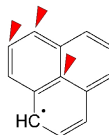
Systems



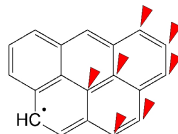
perylene



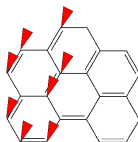
dibenzo[def,mno]crisene /
antranthrene



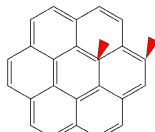
perinaphthenil / fenele



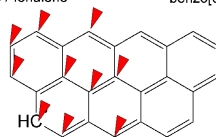
benzo[cd]pirenile



benzo[ghi]perilene



coronene



7 - PAH

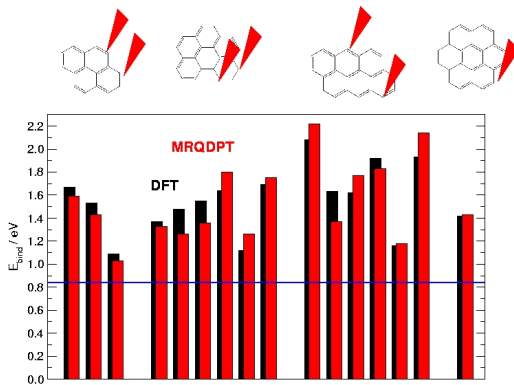
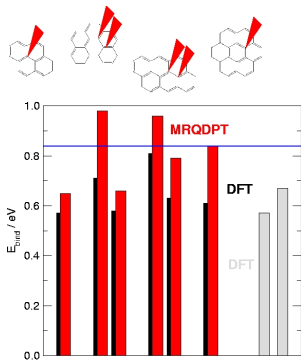
$$\eta = 0$$

$$\eta \neq 0$$





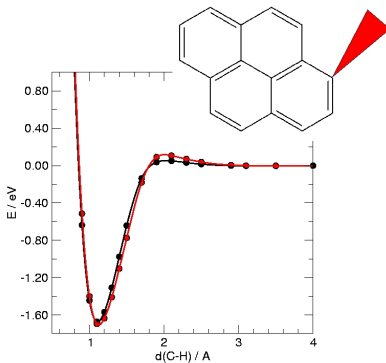
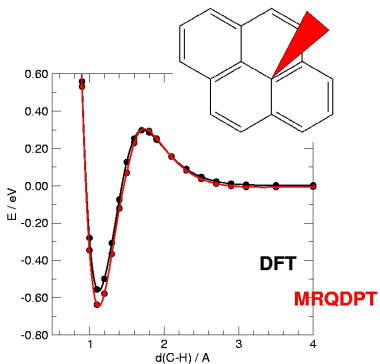
Graphitic vs edge carbons



M. Bonfanti, S. Casolo, G. F. Tantardini, A. Ponti and R. Martinazzo, *J. Chem. Phys.*, **135** 164701 (2011)



Adsorption paths



M. Bonfanti, S. Casolo, G. F. Tantardini, A. Ponti and R. Martinazzo, *J. Chem. Phys.*, **135** 164701 (2011)

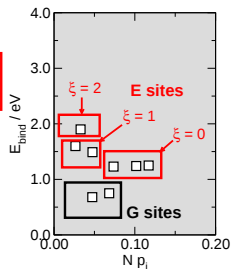
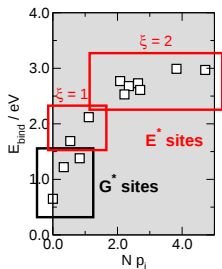
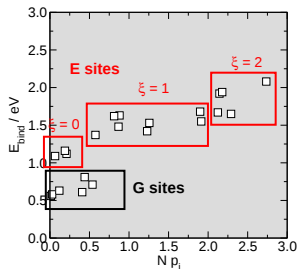




Predicting reactivity

$$\eta = 0$$

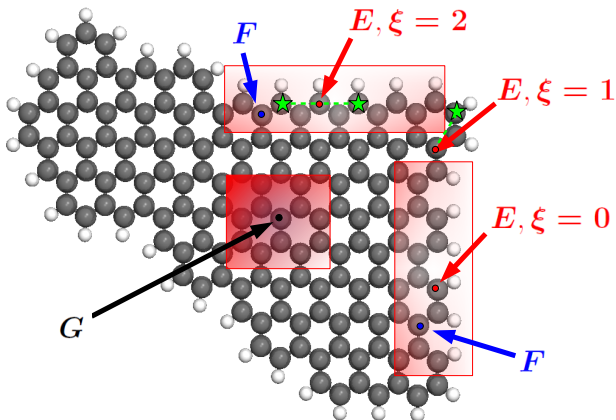
$$\eta \neq 0$$



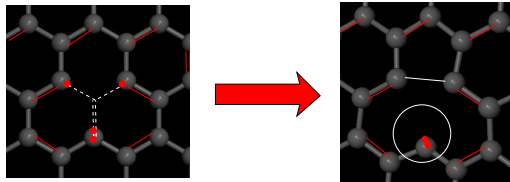
M. Bonfanti, S. Casolo, G. F. Tantardini, A. Ponti and R. Martinazzo, *J. Chem. Phys.*, **135** 164701 (2011)



Predicting reactivity



Spin-coupling around a carbon atom vacancy



How the two e spins couple at a vacancy?

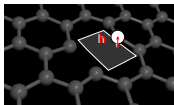
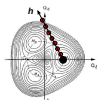
How large is the splitting?

Can that be used in applications?

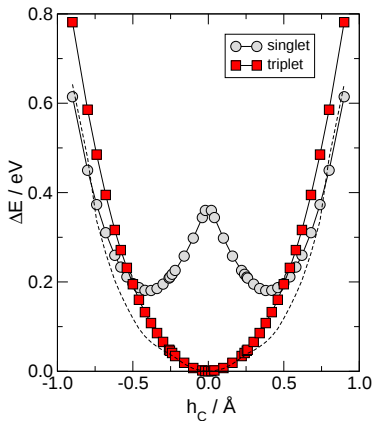


Magnetization constrained results

Partial geometrical relaxation,
 $M_S = 0, 1$ constrained

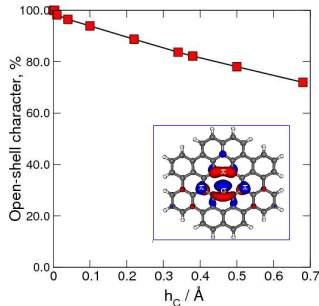
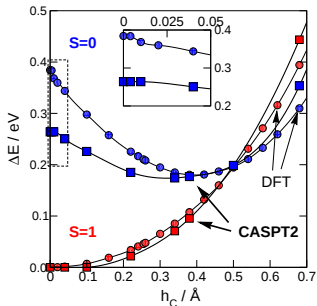


- triplet is stable, $\omega_{\perp} \sim 200 \text{ cm}^{-1}$
- singlet is **bistable**, $\omega_{\perp} \sim 263 \text{ cm}^{-1}$
- $S = 1$ is the ground-state up to $h \sim 0.5 \text{ Å}$





CASPT2 results



- Magnetization constrained DFT results are **reliable**
- **Accurate** energies from CASPT2
- Singlet-state has a dominant **open-shell** character, $\Psi \propto (\sigma\pi + \pi\sigma)(\alpha\beta - \beta\alpha)$

M. Casartelli, S. Casolo, G.F. Tantardini and R. Martinazzo, *submitted*





Outline

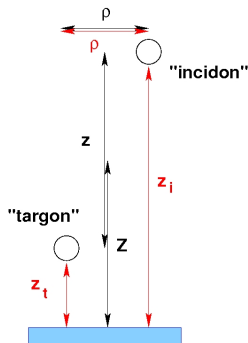
- 1 Point defects in graphene
 - H adsorption and clustering
 - Edge effects
 - Vacancies
- 2 Eley-Rideal reaction
 - Quantum Dynamics at high E_{coll}
 - Quantum Dynamics at cold E_{coll}
 - Ab initio molecular dynamics



Reaction: technicalities

- **Rigid, flat** surface approximation¹
- **Split-Operator** with FFT along cartesian coordinates and DBT along ρ ¹
- propagation in both **product** and **reagent** coordinate sets²

⇒ state-to-state, energy-resolved cross sections for **all** possible processes

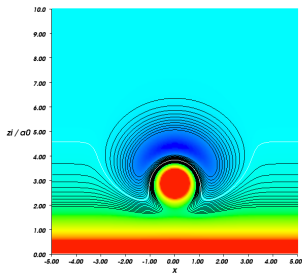


[1] M. Persson and B. Jackson, J. Chem. Phys. 102, 1078 (1995); D. Lemoine and B. Jackson, Comput. Phys. Commun. 137, 415 (2001)

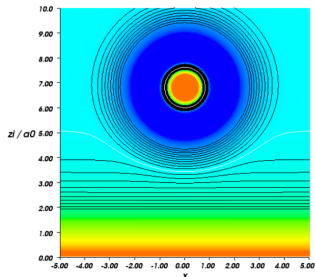
[2] R. Martinazzo and G.F. Tantardini, J. Phys. Chem. A, 109 (2005) 9379; J. Chem. Phys. 124, 124703 (2006); J. Chem. Phys. 124, 124704 (2006)



Reaction: Potential Energy Surfaces



Chemisorbed target H (z_{eq})

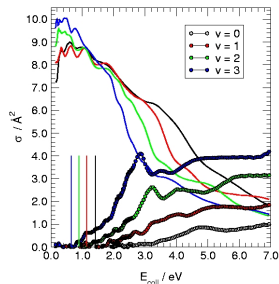
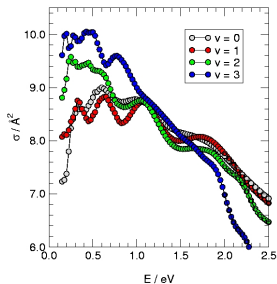


Physisorbed target H (z_{eq})

X. Sha, B. Jackson and D. Lemoine, J. Chem. Phys. 116, 7158 (2002)



I. H-chemisorbed case

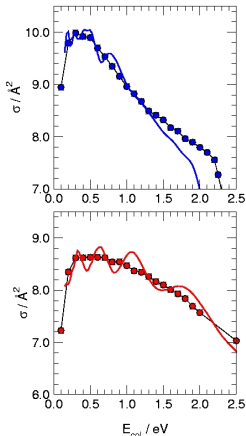
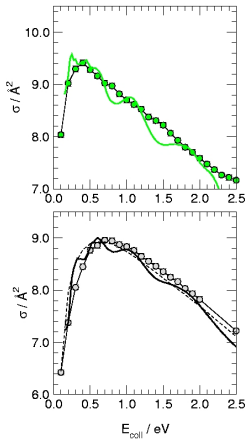


Oscillations in both ER and CID xsections





I. H-chemisorbed case



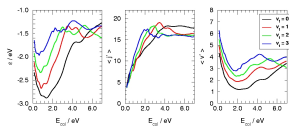
Quantum vs
(quasi) classical
dynamics:
quantum effects

R. Martinazzo and G.F. Tantardini,
J. Phys. Chem. A
109, 9379; *J. Chem. Phys.* **124**
124272 (2006)

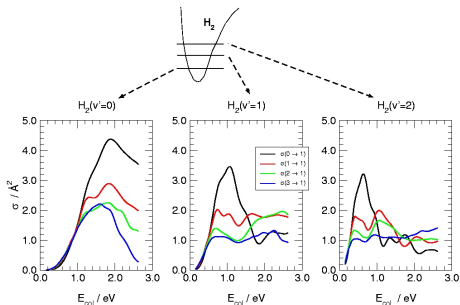




I. H-chemisorbed case

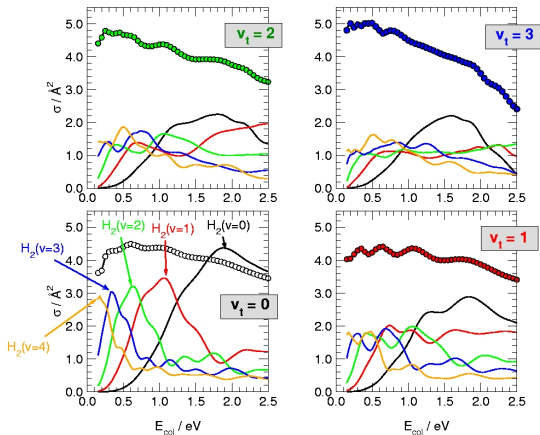


- Product molecules are internally **hot**
- Internal excitation is a steep **decreasing** function of E_{coll}

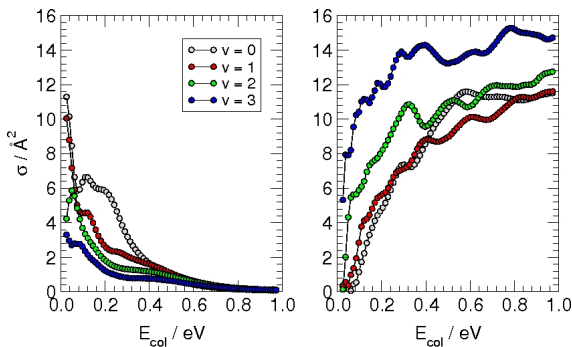




I. H-chemisorbed case



II. H-physisorbed case





Reaction: technicalities (low E_{col})

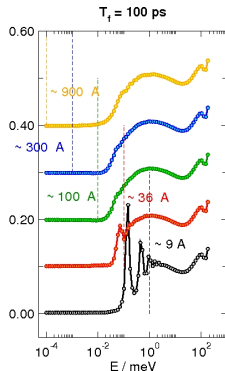
- **Two-wavepacket** approach¹
- **Transmission-free**² absorbing potentials and **Fourier mapping**³ in reagent coordinates

In 3D $T_f=25-30$ ps and AP lengths $\sim 50\text{\AA}$ in order to get converged xsections down to $\sim 10^{-5}$ eV, i.e. ~ 0.1 K

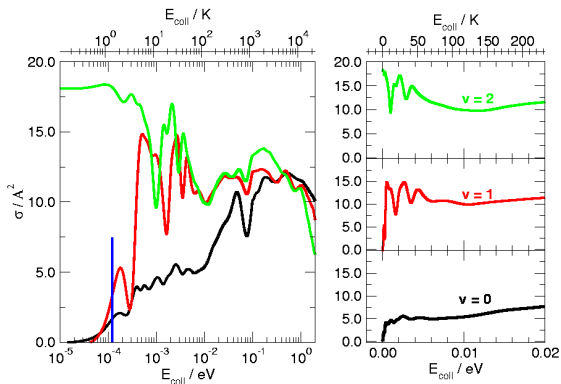
[1] R. Martinazzo and G.F. Tantardini, J. Chem. Phys. 122, 094109 (2005)

[2] D. Manolopoulos, J. Chem. Phys. 117, 9552 (2002)

[3] A.G. Borisov, J. Chem. Phys. 114, 7770 (2001)



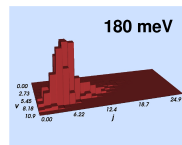
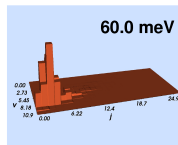
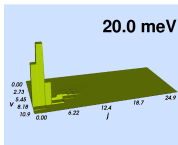
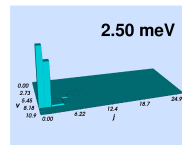
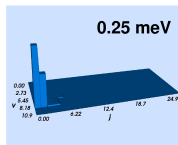
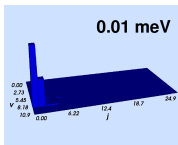
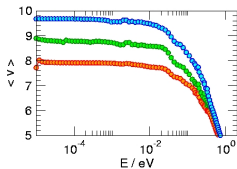
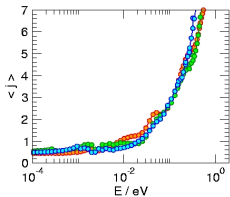
I. H-chemisorbed case



S. Casolo, M. Bonfanti, R. Martinazzo and G.F. Tantardini, *J. Phys. Chem. A*, **113** 14545 (2009)

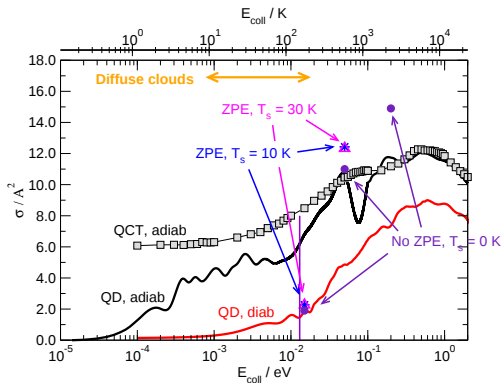


I. H-chemisorbed case



I. H-chemisorbed case

QCT comparison, $\nu = 0$

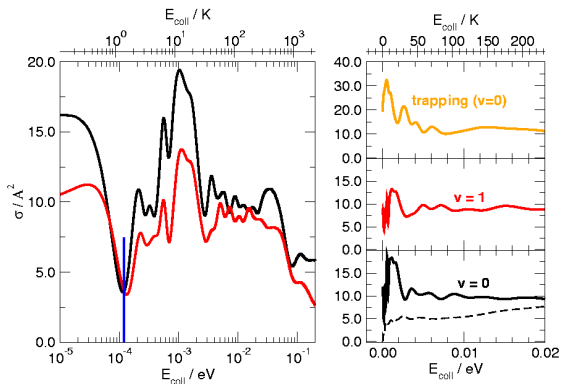


M. Sizun, D. Bachellerie, F. Anguillon, V. Sidis *Chem. Phys. Lett.* **32** **498** 2010

D. Bachellerie, M. Sizun, F. Anguillon, D. Teillet-Billy, N. Rougeau, *Phys. Chem. Chem. Phys.* **2715** **11** 2009



II. H-physisorbed case

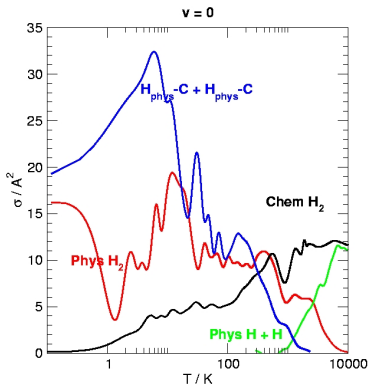


S. Casolo, M. Bonfanti, R. Martinazzo and G.F. Tantardini, *J. Phys. Chem. A*, **113** 14545 (2009)

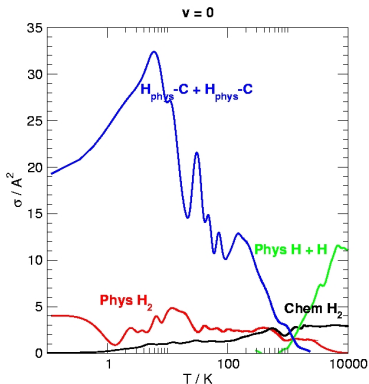




H-chem vs H-phys



H-chem vs H-phys

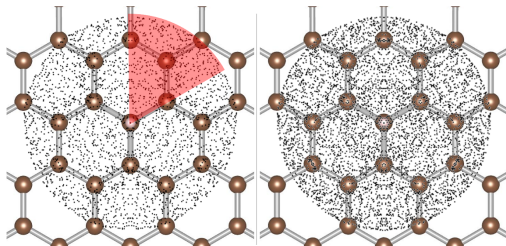


Cross-sections have to be corrected for the **spin** statistics (1/4)



Ab initio molecular dynamics

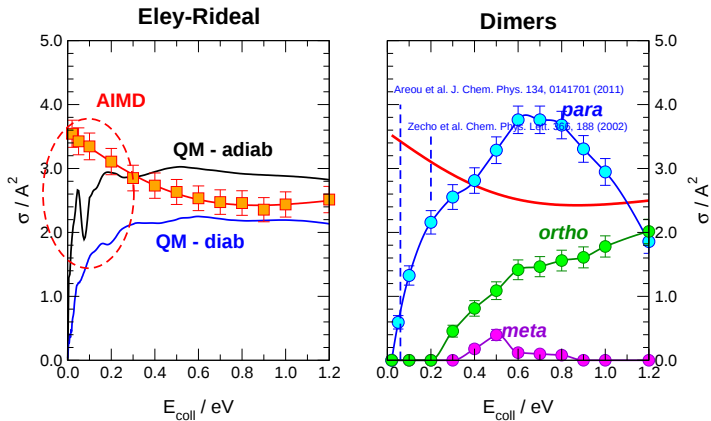
- lattice corrugation
- lattice dynamics
- dimer formation



..expensive, but solves the problem of computing and fitting a model potential

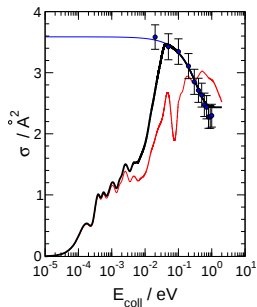
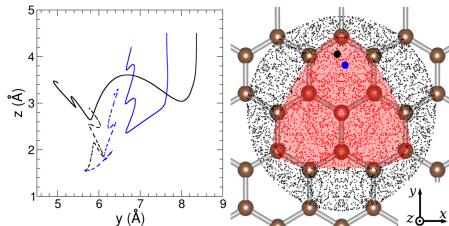


Ab initio molecular dynamics





Ab initio molecular dynamics

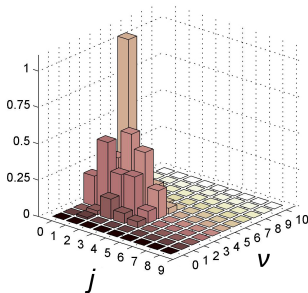
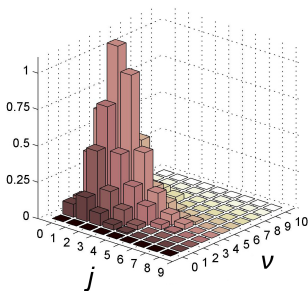


S. Casolo, G.F. Tantardini and R. Martinazzo, PNAS *in press*





Ab initio molecular dynamics



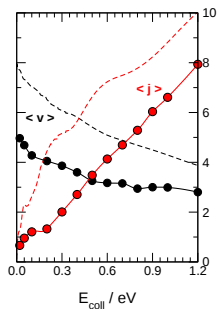
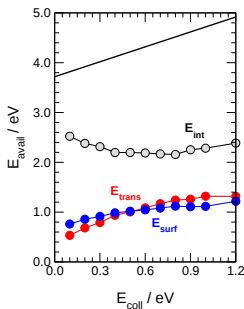
$$T_g = 300K, T_s = 15K$$

Latimer et al. Chem. Phys. Lett. 455, 174 (2008)

AIMD for H/D @ 0.025 eV



Ab initio molecular dynamics



..most of energy is **internal**, but energy transfer to the surface is **considerable**





Summary

- H dimers (clusters) which **minimize** sublattice imbalance form easily in the bulk
- Edges and vacancies are chemically **active** and **facile** sticking is possible at these sites
- **Eley-Rideal** reaction out of **chemisorbed** species is reasonably **efficient**
- and dominates over **dimer formation**
- Product molecules are **hot**, but up to ~ 1 eV can be left on the **surface**



Chemical Dynamics Theory Group

Gian Franco Tantardini



Simone Casolo



Matteo Bonfanti



Simona Achilli



Marina Casartelli



Paolo Bonardi



<http://users.unimi.it/cdtg>



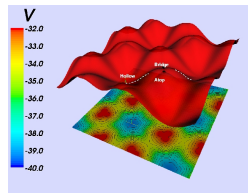
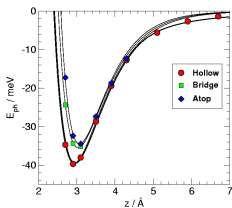


Acknowledgements

Thank you for your attention!



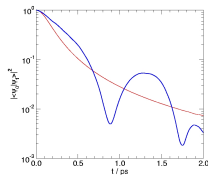
Physisorption



- HF-MP2 / aug-cc-pVDZ + BF_s / CP-BSSE
- $D_e = 39.5 \text{ meV}$ vs $D_e(\text{exp}) = 39.2 \pm 0.5 \text{ meV}$
- $E_{\text{barr}} = 4.0 \text{ meV}$, $D_{T=0K} = 1.7 \cdot 10^{-4} \text{ cm}^2\text{s}^{-1}$

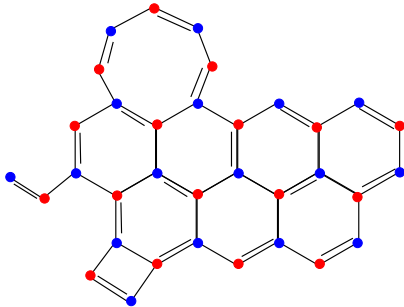
M. Bonfanti, R. Martinazzo, G.F. Tantardini and A. Ponti, *J. Phys. Chem. C*, **111**, 5825 (2007)

Exp: E. Ghio *et al.*, *J. Chem. Phys.*, **73**, 596 (1980)



Midgap states

$$H^\pi \approx \sum_{\sigma, ij} (t_{ij} \mathbf{a}_{i,\sigma}^\dagger \mathbf{b}_{j,\sigma} + t_{ji} \mathbf{b}_{j,\sigma}^\dagger \mathbf{a}_{i,\sigma})$$



Electron-hole symmetry

$$b_i \rightarrow -b_i \implies H_e^\pi \rightarrow -H_e^\pi$$

$$\epsilon_i, |\psi_i^{(+)}\rangle = \sum_k \alpha_k |\mathbf{a}_k\rangle + \sum_j \beta_j |\mathbf{b}_j\rangle$$

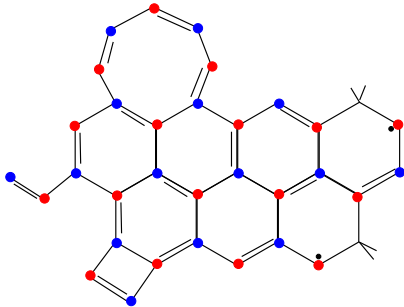
$\Downarrow$

$$-\epsilon_i, |\psi_i^{(-)}\rangle = \sum_k \alpha_k |\mathbf{a}_k\rangle - \sum_j \beta_j |\mathbf{b}_j\rangle$$



Midgap states

$$H^\pi \approx \sum_{\sigma, ij} (t_{ij} a_{i,\sigma}^\dagger b_{j,\sigma} + t_{ji} b_{j,\sigma}^\dagger a_{i,\sigma})$$



Imbalance rule

Let $n_A > n_B$, $\mathbf{T}(n_B \times n_A)$

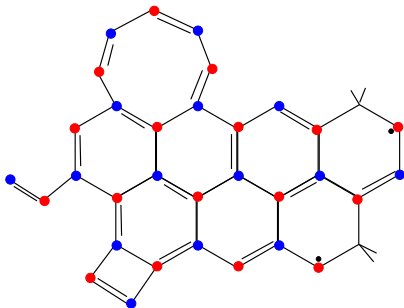
$$\begin{bmatrix} \mathbf{0} & \mathbf{T}^\dagger \\ \mathbf{T} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix}$$

$\Rightarrow \mathbf{T}\alpha = \mathbf{0}$ has $n_A - n_B$ solutions



Midgap states

$$H^\pi \approx \sum_{\sigma, ij} (t_{ij} a_{i,\sigma}^\dagger b_{j,\sigma} + t_{ji} b_{j,\sigma}^\dagger a_{i,\sigma}) + U \sum_i n_{i,\uparrow} n_{i,\downarrow}$$



Spin alignment

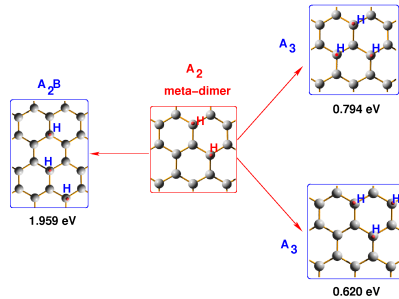
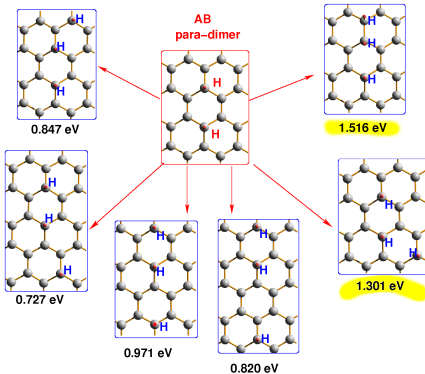
If $U > 0$, the ground-state at *half-filling* has

$$S = |n_A - n_B|/2 = n_I/2$$

E.H. Lieb, *Phys. Rev. Lett.* **62**, 1201 (1989)



3-atom clusters



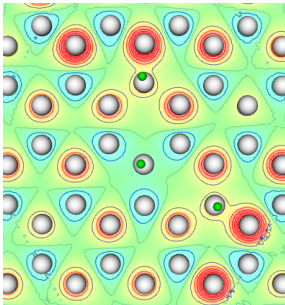
$$\mu = 1\mu_B \Rightarrow \mu = 2\mu_B \Rightarrow \mu = 3\mu_B$$

$$\mu = 1\mu_B \Rightarrow \mu = 2\mu_B \Rightarrow \mu = 3\mu_B$$

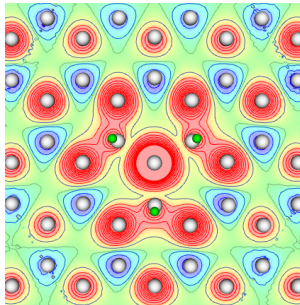


3-atom clusters

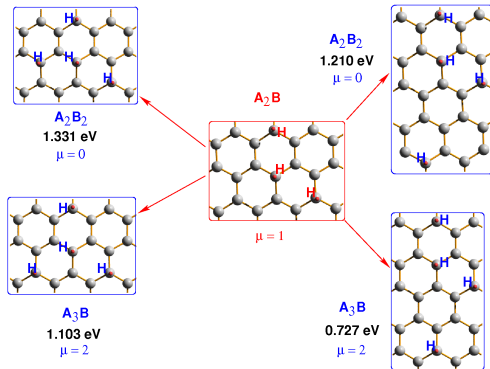
A_2B



A_3

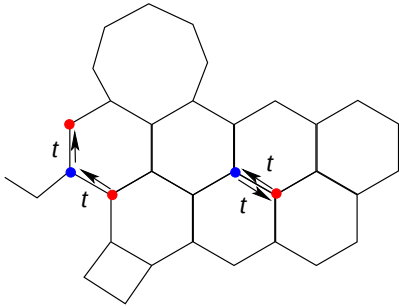


4-atom clusters



Hints from the tight-binding Hamiltonian H^π

$$H^\pi \approx \sum_{\sigma, ij} (t_{ij} a_{i,\sigma}^\dagger b_{j,\sigma} + t_{ji} b_{j,\sigma}^\dagger a_{i,\sigma})$$



‘Lattice renormalization’

$$\tilde{H}_{AA} = H_{AB} H_{BA}$$

$$\tilde{\epsilon}_i, |\psi_{A,i}\rangle$$

$\Downarrow$

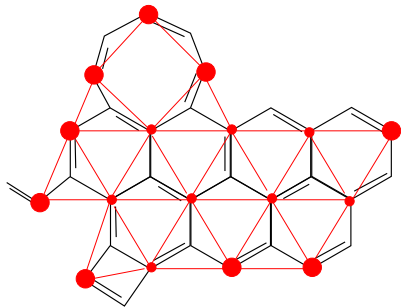
$$\epsilon_i^\pm = \pm \sqrt{\tilde{\epsilon}_i}, |\psi_i^{(\pm)}\rangle = |\psi_{A,i}\rangle \pm |\psi_{B,i}\rangle$$

$$|\psi_{B,i}\rangle = \tilde{\epsilon}_i^{-1/2} H_{BA} |\psi_{A,i}\rangle$$



Hints from the tight-binding Hamiltonian H^π

$$\tilde{H}^\pi \approx \sum_i Z_i t^2 \mathbf{a}_i^\dagger \mathbf{a}_i + \sum_{ij} t^2 \mathbf{a}_i^\dagger \mathbf{a}_j$$



‘Lattice renormalization’

$$\tilde{H}_{AA} = H_{AB} H_{BA}$$

$$\tilde{\epsilon}_i, |\psi_{A,i}\rangle$$

$\downarrow$

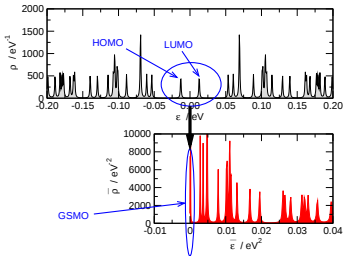
$$\epsilon_i^\pm = \pm \sqrt{\tilde{\epsilon}_i}, |\psi_i^{(\pm)}\rangle = |\psi_{A,i}\rangle \pm |\psi_{B,i}\rangle$$

$$|\psi_{B,i}\rangle = \tilde{\epsilon}_i^{-1/2} H_{BA} |\psi_{A,i}\rangle$$



Hints from the tight-binding Hamiltonian H^π

$$\tilde{H}^\pi \approx \sum_i Z_i t^2 \mathbf{a}_i^\dagger \mathbf{a}_i + \sum_{ij} t^2 \mathbf{a}_i^\dagger \mathbf{a}_j$$



'Lattice renormalization'

$$\tilde{H}_{AA} = H_{AB} H_{BA}$$

$$\tilde{\epsilon}_i, |\psi_{A,i}\rangle$$

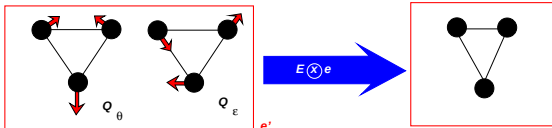
$\Downarrow$

$$\epsilon_i^\pm = \pm \sqrt{\tilde{\epsilon}_i}, |\psi_i^{(\pm)}\rangle = |\psi_{A,i}\rangle \pm |\psi_{B,i}\rangle$$

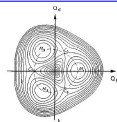
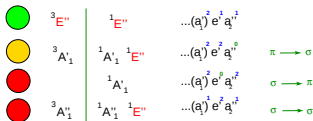
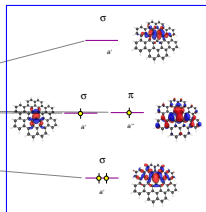
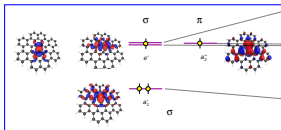
$$|\psi_{B,i}\rangle = \tilde{\epsilon}_i^{-1/2} H_{BA} |\psi_{A,i}\rangle$$



$E \otimes e$ JT problem

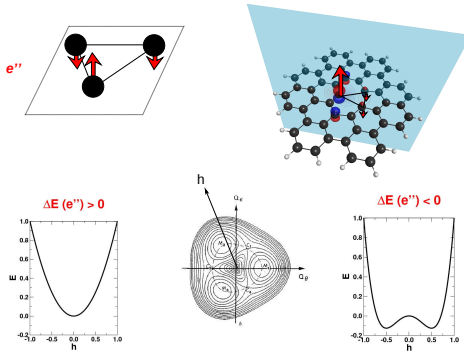


$$[E''^2] = [E'^2] = A' + E'$$



..with interacting higher-energy states

Out-of-plane, E'' vibrations do not lift degeneracy at first order..



..but give corrections to second order, either **positive** or **negative** *



Zecho's kinetic experiments

